

Sawn Timber

P_r is the lesser of:

$$P_{rd} = \phi F_c A K_{Zcd} K_{cd} \text{ or } P_{rb} = \phi F_c A K_{Zcb} K_{cb}$$

where:

ϕF_c = factored compressive resistance strength (MPa) given in Table 3.6

K_{Zc} = size factor

$$K_{Zcd} = 6.3 (dL_d)^{-0.13} \leq 1.3 \text{ for buckling in direction of } d$$

$$K_{Zcb} = 6.3 (bL_b)^{-0.13} \leq 1.3 \text{ for buckling in direction of } b$$

K_C = slenderness factor

$$K_{Cd} = \left[1.0 + \frac{F_c}{E'} K_{Zcd} C_{cd}^3 \right]^{-1} \text{ for buckling in direction of } d$$

$$K_{Cb} = \left[1.0 + \frac{F_c}{E'} K_{Zcb} C_{cb}^3 \right]^{-1} \text{ for buckling in direction of } b$$

F_c/E' = strength to stiffness ratio given in Table 3.7

$$C_{cd} = \frac{K_e L_d}{d} \quad C_{cb} = \frac{K_e L_b}{b} \quad (C_{cd} \text{ or } C_{cb} > 50 \text{ is not permitted})$$

K_e = effective length factor, given in Figure 3.1

L_b, L_d = unsupported length associated with d or b (mm)

d = depth of member (mm)

b = thickness of member (mm)

Glulam

$$P_r = \phi F_c A K_{Zcg} K_C$$

where:

ϕF_c = factored compressive resistance strength (MPa) given in Table 3.8

$$K_{Zcg} = 0.68 (Z)^{-0.13} \leq 1.0, \text{ where } Z = \text{member volume in } m^3$$

K_C = slenderness factor

$$= \left[1.0 + \frac{F_c}{E'} K_{Zcg} C_c^3 \right]^{-1}$$

F_c/E' = strength to stiffness ratio given in Table 3.9

$$C_c = \text{the greater of } \frac{K_e L_d}{d} \text{ or } \frac{K_e L_b}{b} \quad (C_c > 50 \text{ is not permitted})$$

K_e = effective length factor, given in Figure 3.1

L_b, L_d = unsupported length associated with d or b (mm)

d = depth of member (mm)

b = thickness of member (mm)

1. The studs must be designed to satisfy the following interaction equation

$$\left(\frac{P_f}{P_r}\right)^2 + \frac{M_f}{M_r} \left[\frac{1}{1 - \frac{P_f}{P_E}} \right] \leq 1.0$$

where:

P_f = factored axial load on stud (N)

P_r = factored compressive resistance parallel to grain taken from Table 9.17 ($K_D = 1.0$) ($K_T = 0.75$) (N)

M_f = maximum factored bending moment

$$\frac{w_f H^2}{6L} \left[L - H + \frac{2}{3} \sqrt{\frac{H^3}{3L}} \right]$$

w_f = factored loading (N/mm)

= 1.5 x specified lateral soil pressure (kN/m²) x stud spacing (m)

M_r = factored bending moment resistance taken from Joist Selection Tables in 2.3 modified for permanent load duration ($K_D = 0.65$) and treatment factor for preservation treated, incised lumber used in dry service conditions ($K_T = 0.75$) (kN•m)

2. Maximum deflection under specified loads $\leq$ deflection criteria (actual $E_s I \geq$ required $E_s I$)

Maximum deflection, Δ , may be calculated using the formula given below:

$$\Delta = \frac{w(L-x)}{360(E_s I) L H} K_{\Delta} \text{ (mm)}$$

where:

w = specified lateral soil pressure (kN/m²) x stud spacing (m)

$$K_{\Delta} = 10 H^3 (2L-x)x - 3H^5 + K_2$$

$$K_2 = \frac{3L}{L-x} (H-x)^5 \text{ when } x \leq H$$

$$K_2 = 0 \text{ when } x > H$$

$$x = 0.45L$$

$E_s I$ = bending stiffness taken from Joist Selection Tables and modified by the treatment factor for preservative treated, incised lumber used in dry service conditions ($K_T = 0.9$) (N•mm²)

Generally, $L/300$ is used as the deflection criteria.

Notice to Purchasers of the Wood Design Manual Concerning Equivalency Between Spruce-Pine-Fir and Southern Pine Dimension Lumber

Design values for some grades and sizes of Southern Pine visually graded lumber, published by the Southern Pine Inspection Bureau (SPIB) have been reduced. The American Lumber Standards Committee Board of Review has approved these changes to take effect June 1st 2012.

SPIB is currently reviewing design values for all sizes and grades and it is expected that there will be further changes to Southern Pine design values.

A CSA O86 Technical Committee ballot is currently being conducted to approve an amendment that would remove the equivalency between Southern Pine and Spruce-Pine-Fir in Table 5.2.1.3 of CSA O86 until the outcome of SPIB's review is completed:

Table 5.2.1.3
Lumber species equivalents

US combination	Equivalent Canadian combination
Douglas Fir-Larch	Douglas Fir-Larch
Hem-Fir	Hem-Fir
Southern Pine	Spruce Pine Fir

Note: The NLGA Standard Grading Rules for Canadian Lumber incorporates the National Grading Rule for Dimension Lumber, a uniform set of grade descriptions and other requirements for softwood dimension lumber that form a required part of all softwood lumber grading rules in the United States. Thus, all dimension lumber throughout Canada and the United States is graded to uniform requirements.

The ballot can be reviewed at <http://publicreview.csa.ca/>

The result of the ballot will be circulated once the ballot has been completed

Further information can be found on the SPIB website at <http://www.spib.org/important-notice.shtml>

Update No. 4

O86-09

September 2012

Note: For information about the **Standards Update Service** or if you are missing any updates, go to **shop.csa.ca** or e-mail **techsupport@csagroup.org**.

Title: *Engineering design in wood* — originally published May 2009

Revisions issued: Update No. 1 — September 2010
Update No. 2 — March 2011
Update No. 3 — December 2011 (applies to the French Standard only)

The following revisions have been formally approved and are marked by the symbol delta (Δ) in the margin on the attached replacement pages:

Revised	Clause 10.11.4.2 and Tables 5.2.1.3 and 10.3.4
New	None
Deleted	None

- Update your copy by inserting these revised pages.
- Keep the pages you remove for reference.

Δ

Table 5.2.1.3
Lumber species equivalents

US combination	Equivalent Canadian combination
Douglas Fir-Larch	Douglas Fir-Larch
Hem-Fir	Hem-Fir

Note: The NLGA's Standard Grading Rules for Canadian Lumber incorporates the National Grading Rule for Dimension Lumber, a uniform set of grade descriptions and other requirements for softwood dimension lumber that form a required part of all softwood lumber grading rules in the United States. Thus, all dimension lumber throughout Canada and the United States is graded to uniform requirements.

5.2.2 Lumber grades and categories

5.2.2.1 Visually stress-graded lumber

Table 5.2.2.1 lists categories, limiting dimensions, and structural grades for which design data are assigned in this Standard. These grades are specified in the NLGA's *Standard Grading Rules for Canadian Lumber*.

Table 5.2.2.1
Visual grades and their dimensions

Grade category	Smaller dimension, mm	Larger dimension, mm	Grades
Light framing	38 to 89	38 to 89	Construction, Standard
Stud	38 to 89	38 or more	Stud
Structural light framing	38 to 89	38 to 89	Select Structural No. 1, No. 2, No. 3
Structural joists and planks	38 to 89	114 or more	Select Structural No. 1, No. 2, No. 3
Beam and stringer	114 or more	Exceeds smaller dimension by more than 51	Select Structural No. 1, No. 2
Post and timber	114 or more	Exceeds smaller dimension by 51 or less	Select Structural No. 1, No. 2
Plank decking	38 to 89	140 or more	Select, Commercial

5.2.2.2 Machine stress-rated (MSR) and machine evaluated lumber (MEL)

The design data specified in this Standard apply to lumber graded and grade-stamped in accordance with NLGA SPS 2 and identified by the grade stamp of a grading agency accredited for grading by mechanical means.

Note: A list of accredited agencies can be obtained from the Canadian Lumber Standards Accreditation Board.

5.2.3 Finger-joined lumber

5.2.3.1

The design data specified in this Standard apply to finger-joined lumber that has been produced and grade-stamped in accordance with NLGA SPS 1.

5.2.3.2

The design data specified in this Standard apply to finger-joined lumber that has been produced and grade-stamped in accordance with NLGA SPS 3 where used under the following conditions:

- (a) applications where the primary loading is in compression, with only short-duration stresses in bending or tension, such as due to wind or earthquake loads; and
- (b) protected from wet service conditions at all times and not used in environments where the equilibrium moisture content can be expected to exceed 19% or the temperature can be expected to exceed 50 °C for an extended period of time.

5.2.4 Remanufactured lumber

Dimension lumber and timbers that are resawn or otherwise remanufactured shall be regraded in accordance with Clause 5.2.1.

5.2.5 Mixed grades

When mixed grades are used, the specified strength shall be that of the grade having the lowest value.

5.3 Specified strengths

5.3.1 Visually stress-graded lumber

5.3.1.1

The specified strengths (MPa) for visually stress-graded lumber are tabulated as follows:

- (a) structural joist and plank, structural light framing, and stud grade categories of lumber in Table 5.3.1A;
- (b) light framing grades in Table 5.3.1B;
- (c) beam and stringer grade categories of lumber in Table 5.3.1C; and
- (d) post and timber grade categories of lumber in Table 5.3.1D.

5.3.1.2

The specified strengths (MPa) for plank decking shall be derived from Table 5.3.1A using the following grade equivalents:

Decking grade	Equivalent lumber grade
Select	Select structural
Commercial	No. 2

5.3.2 Machine stress-rated and machine evaluated lumber

The specified strengths (MPa) for machine stress-rated lumber are given in Table 5.3.2. The specified strengths (MPa) for machine evaluated lumber are given in Table 5.3.3. Specified strengths in shear are not grade dependent and shall be taken from Table 5.3.1A for the appropriate species.

10.3.4 Lumber thickness

Connectors installed in lumber of a thickness less than the minimum specified in Table 10.3.4 for the connector type and use shall not be considered to provide resistance.

Δ

Table 10.3.4
Thickness factor for timber connector, J_T

Connector type and size	Number of faces of a piece containing connectors on a bolt	Thickness of piece, mm	J_T
2-1/2 in split ring	1	38	1.00
		25	0.85
	2	51	1.00
		38	0.80
4 in split ring	1	38	1.00
		25	0.65
	2	76	1.00
		64	0.95
		51	0.80
		38	0.65
2-5/8 in shear plate	1	64	1.00
		51	0.95
		38	0.95
	2	64	1.00
		51	0.95
		38	0.75
4 in shear plate	1	44	1.00
		38	0.85
	2	89	1.00
		76	0.95
		64	0.85
		51	0.75
		44	0.65

10.3.5 Lag screw connector joints

When lag screws instead of bolts are used with connectors, the resistance shall vary uniformly with penetration into the member receiving the point, from the full resistance for one connector unit with bolt for standard penetration to 0.75 times the full resistance for one connector unit with bolt for minimum penetration. Penetration shall be as specified in Table 10.3.5 and shall be not less than the minimum value.

Table 10.3.5
Penetration factor, J_p , for split rings and
shear plates used with lag screws

		Penetration of lag screw into member receiving point (number of shank diameters)				
		Species				
Connector	Penetration	Douglas Fir-Larch	Hem-Fir	Spruce-Pine-Fir	Northern Species	J_P
2-1/2 in split ring	Standard	8	10	10	11	1.00
4 in split ring or 4 in shear plate*	Minimum	3.5	4	4	4.5	0.75
2-5/8 in shear plate*	Standard	5	7	7	8	1.00
	Minimum	3.5	4	4	8	0.75

*When steel side plates are used with shear plates, use $J_p = 1.0$.

Note: For intermediate penetrations, linear interpolation may be used for values of J_p between 0.75 and 1.00.

10.3.6 Lateral resistance

The factored lateral strength resistance of a split ring or shear plate connection, P_r , Q_r , or N_r , determined using the equations specified in this Clause, shall be greater than or equal to the effect of the factored loads. The factored strength resistance per shear plate unit shall not exceed the values specified in Table 10.3.6C.

(a) For parallel-to-grain loading:

$$P_r = \phi P_u n_F / F$$

(b) For perpendicular-to-grain loading:

$$Q_r = \phi Q_u n_F / F$$

(c) For loads at angle θ to grain:

$$N_r = \frac{P_r Q_r}{P_r \sin^2 \theta + Q_r \cos^2 \theta}$$

where

$$\phi = 0.6$$

$$P_u = p_u (K_D K_{SF} K_T)$$

where

p_u = lateral strength resistance parallel to grain, kN (Table 10.3.6A)

$$J_F = J_G J_C J_T J_O J_P$$

where

J_G = factor for groups of fastenings (Tables 10.2.2.3.4A and 10.2.2.3.4B)

J_C = minimum configuration factor (Clause 10.3.3 and Tables 10.3.3A to 10.3.3C)

J_T = thickness factor (Table 10.3.4)

J_O = factor for connector orientation in grain

= 1.00 for side grain installation

= 0.67 for end grain and all other installations

J_P = factor for lag screw penetration (Clause 10.3.5 and Table 10.3.5)

10.11.3.2

The factored withdrawal resistance of a single wood screw per millimetre of threaded shank penetration when driven perpendicular to the grain shall be determined in accordance with Clause 10.11.5. Wood screws installed through end grain shall not be considered to carry load in withdrawal.

10.11.4 Lateral resistance

10.11.4.1

For two- or three-member joints, the factored lateral strength resistance of a wood screw joint shall be taken as follows:

$$N_r = \phi N_u n_f n_s J_A J_E$$

where

$$\phi = 0.8$$

$$N_u = n_u (K_D K_{SF} K_T)$$

where

n_u = unit lateral strength resistance, N (Clause 10.11.4.2)

n_f = number of fasteners in the connection

n_s = number of shear planes per screw

J_A = toe-screwing factor

= 0.83 where screws are started at approximately one-third the screw length from the end of a piece and driven at an angle of about 30° to the grain of the member

= 1.0 in all other cases

J_E = factor for fastening into end grain

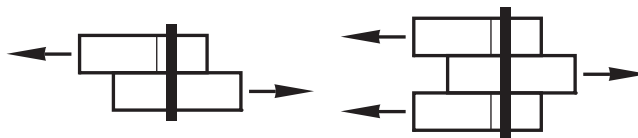
= 0.67 in end grain

= 1.0 in all other cases

10.11.4.2

The unit lateral strength resistance, n_u (N per shear plane), shall be taken as the smallest value calculated in accordance with Items (a) to (g). For two-member connections, only Items (a), (b), (d) to (f), and (g) are valid. For three-member connections, where screws fully penetrate all three members, only Items (a), (c), (d), and (g) are valid.

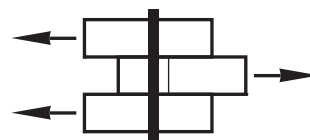
(a) $f_1 d_f t_1$



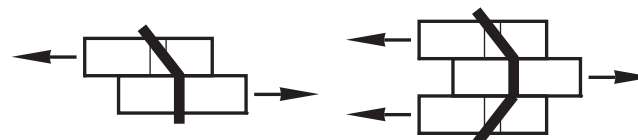
(b) $f_2 d_f t_2$



(c) $\frac{1}{2} f_2 d_f t_2$



(d) $f_1 d_f^2 \left(\sqrt{\frac{1}{6} \frac{f_3}{(f_1 + f_3)} \frac{f_y}{f_1} + \frac{1}{5} \frac{t_1}{d_f}} \right)$



$$\begin{aligned}
 \text{(e)} \quad & f_1 d_f^2 \left(\sqrt{\frac{1}{6} \frac{f_3}{(f_1 + f_3)} \frac{f_y}{f_1} + \frac{1}{5} \frac{t_2}{d_f}} \right) \quad \begin{array}{c} \leftarrow \text{Diagram 1} \rightarrow \\ \leftarrow \text{Diagram 2} \rightarrow \end{array} \\
 \text{(f)} \quad & f_1 d_f^2 \frac{1}{5} \left(\frac{t_1}{d_f} + \frac{f_2}{f_1} \frac{t_2}{d_f} \right) \quad \begin{array}{c} \leftarrow \text{Diagram 3} \rightarrow \\ \leftarrow \text{Diagram 4} \rightarrow \end{array} \\
 \text{(g)} \quad & f_1 d_f^2 \sqrt{\frac{2}{3} \frac{f_3}{(f_1 + f_3)} \frac{f_y}{f_1}} \quad \begin{array}{c} \leftarrow \text{Diagram 5} \rightarrow \\ \leftarrow \text{Diagram 6} \rightarrow \end{array}
 \end{aligned}$$

where

d_f = wood screw diameter, mm (Table 10.11.1)

t_1 = head-side member thickness for two-member connections, mm

= minimum side plate thickness for three-member connections, mm (Clause 10.11.2.3)

f_2 = embedding strength of main member where failure is wood bearing, MPa

= $50 G (1 - 0.01 d_f)$

where

G = mean relative density of lumber or glulam member (see Table A.10.1)

t_2 = length of penetration into point-side member for two-member connections, mm

= centre member thickness for three-member connections, mm (Clause 10.11.2.3)

f_3 = embedding strength of main member where failure is fastener yielding, MPa

= $110 G^{1.8} (1 - 0.01 d_f)$

f_y = wood screw yield strength, MPa (Table 10.11.1)

For lumber side plates:

f_1 = embedding strength, MPa

= $50 G (1 - 0.01 d_f)$

For structural panel side plates:

f_1 = embedding strength, MPa

= $104 G (1 - 0.1 d_f)$

where

Δ $G = 0.49$ for DFP

= 0.42 for CSP and OSB

For steel side plates:

f_1 = embedding strength of steel side plate, MPa

= $K_{sp} (\phi_{steel} / \phi_{wood}) f_u$

where

K_{sp} = 3.0 for mild steel meeting the requirements of CSA G40.21 or ASTM A 36/A 36M

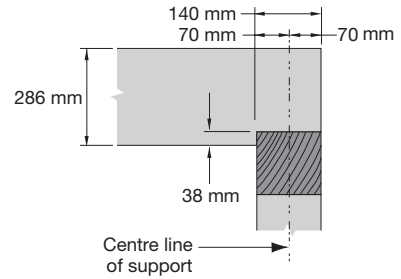
= 2.7 for light gauge steel

ϕ_{steel} = resistance factor for steel member in wood screw connection

Example 2: Joists notched on tension side at supports

Verify that the Hem-Fir No.1/No.2 38 × 286 mm floor joists (see drawing) notched at the supports are adequate for the following conditions:

- joist spacing = 600 mm
- joist span = 4.0 m
- specified dead load = 1.2 kPa
- specified live load = 2.4 kPa
- standard load duration
- dry service conditions
- untreated
- fully laterally supported by subfloor
- Case 2 system

**Calculation**

Total factored load = $(1.25 \times 1.20) + (1.5 \times 2.40) = 5.10$ kPa

Total specified load = $1.20 + 2.40 = 3.60$ kPa

$$w_f = 5.10 \times 0.6 = 3.06 \text{ kN/m}$$

$$w = 3.60 \times 0.6 = 2.16 \text{ kN/m}$$

$$w_L = 2.40 \times 0.6 = 1.44 \text{ kN/m}$$

$$M_f = \frac{w_f L^2}{8} = \frac{3.06 \times 4.0^2}{8} = 6.12 \text{ kN}\cdot\text{m}$$

$$V_f = \frac{w_f L}{2} = \frac{3.06 \times 4.0}{2} = 6.12 \text{ kN}$$

$$A_n = 9424 \text{ mm}^2$$

$$A = 10870 \text{ mm}^2$$

$$A_n/A = 0.87$$

Note: In this example, the maximum factored reaction force Q_f is equal to V_f .

From the Serviceability Table:

$$E_S I_{REQ'D} = 432 \times 10^9 \text{ N}\cdot\text{mm}^2 \text{ for } L/360 \text{ deflection based on live load } (w_L)$$

From Joist Selection Tables:

$$M_r = 7.18 > 6.12 \text{ kN}\cdot\text{m}$$

Acceptable

$$V_r = 14.6 \times 0.87 = 12.70 > 6.12 \text{ kN}$$

Acceptable

$$E_S I = 815 \times 10^9 > 432 \times 10^9 \text{ N}\cdot\text{mm}^2$$

Acceptable



The factored notch shear force resistance at the support:

$$F_r = \phi F_f A K_N$$

$$\phi = 0.9$$

$$F_f = 0.5 \times 1.4 = 0.7 \text{ MPa}$$

$$A = 38 \times 286 = 10868 \text{ mm}^2$$

$$K_N = \left[0.006 d \left[1.6 \left[\frac{1}{\alpha} - 1 \right] + \eta^2 \left[\frac{1}{\alpha^3} - 1 \right] \right] \right]^{-0.5}$$

$$\alpha = 1 - \frac{d_n}{d} = 1 - \frac{38}{286} = 0.24$$

$$\eta = \frac{e}{d} = \frac{70}{286} = 0.87$$

$$K_N = \left[0.006 \times 286 \left[1.6 \left[\frac{1}{0.87} - 1 \right] + 0.24^2 \left[\frac{1}{0.87^3} - 1 \right] \right] \right]^{-0.5} = 1.45$$

Note: As an alternative, K_N may also be calculated using Table 5.5.5.4 of CSA O86.

Therefore:

$$\begin{aligned} F_r &= 0.9 \times 0.7 \times 10868 \times 1.45 \\ &= 9.93 \text{ kN} > Q_f = 6.12 \text{ kN} \end{aligned}$$

Acceptable

Note: Also verify acceptable bearing capacity as per Chapter 6.

Column Selection Tables

Glulam

365 mm

L m	Spruce-Pine 12c-E								D.Fir-L 16c-E							
	d (mm) 342		380		418		456		342		380		418		456	
	P_{rx} kN	P_{ry} kN	P_{rx} kN	P_{ry} kN	P_{rx} kN	P_{ry} kN	P_{rx} kN	P_{ry} kN	P_{rx} kN	P_{ry} kN	P_{rx} kN	P_{ry} kN	P_{rx} kN	P_{ry} kN	P_{rx} kN	P_{ry} kN
2.0	2020	2030	2220	2220	2420	2410	2620	2600	2420	2430	2670	2660	2900	2890	3140	3120
2.5	1940	1950	2140	2140	2340	2320	2530	2500	2330	2340	2570	2560	2800	2790	3030	3010
3.0	1860	1880	2060	2060	2260	2240	2450	2410	2240	2250	2480	2470	2710	2680	2940	2900
3.5	1780	1800	1990	1980	2190	2150	2380	2320	2140	2170	2390	2380	2630	2590	2860	2790
4.0	1700	1730	1910	1900	2120	2060	2310	2230	2050	2080	2300	2280	2540	2480	2780	2680
4.5	1610	1650	1830	1810	2040	1970	2240	2130	1950	1990	2210	2190	2460	2380	2690	2570
5.0	1530	1570	1750	1720	1960	1880	2170	2030	1850	1900	2110	2080	2370	2270	2610	2450
5.5	1430	1490	1670	1630	1880	1780	2090	1920	1740	1800	2020	1980	2280	2150	2520	2330
6.0	1340	1400	1580	1540	1800	1680	2020	1810	1630	1700	1910	1870	2180	2040	2430	2200
6.5	1250	1320	1490	1450	1720	1580	1940	1710	1520	1600	1810	1760	2080	1920	2340	2080
7.0	1160	1230	1400	1350	1630	1480	1860	1600	1420	1500	1710	1650	1980	1800	2250	1950
7.5	1070	1140	1310	1260	1550	1380	1770	1490	1310	1400	1600	1540	1880	1680	2150	1820
8.0	982	1060	1220	1170	1460	1280	1690	1380	1210	1300	1500	1440	1780	1570	2050	1700
8.5	901	983	1140	1080	1370	1180	1600	1280	1110	1210	1400	1330	1680	1460	1960	1580
9.0	826	908	1060	1000	1290	1090	1520	1190	1020	1120	1300	1240	1580	1350	1860	1460
9.5	755	837	979	923	1210	1010	1440	1090	937	1040	1210	1140	1480	1250	1760	1350
10.0	690	770	905	850	1130	930	1360	1010	858	955	1120	1050	1390	1150	1670	1250
10.5	630	708	836	782	1050	856	1280	929	786	880	1040	972	1300	1060	1570	1150
11.0	576	651	772	719	983	787	1200	855	719	810	959	895	1220	980	1480	1060
11.5	526	598	712	661	916	724	1130	786	658	746	887	825	1130	903	1390	980
12.0	481	549	657	607	852	665	1060	723	603	687	819	759	1060	831	1310	903
12.5	440	505	606	559	793	612	994	665	552	632	757	699	986	766	1230	833
13.0	403	464	559	514	737	563	931	612	506	582	700	644	918	706	1160	767
13.5	369	427	516	473	685	518	872	564	464	537	647	594	855	651	1080	708
14.0	339	393	476	436	637	478	816	520	427	495	598	548	796	601	1020	653
14.5	311	363	440	402	592	441	764	479	392	457	554	506	742	555	953	603
15.0	286	335	407	371	551	407	715	443	361	422	513	467	691	513	893	558

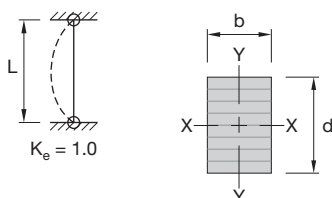
3



Compression Members

Notes:

- P_{rx} is the factored resistance to buckling about the x-x (strong) axis.
 P_{ry} is the factored resistance to buckling about the y-y (weak) axis.
- For $L \leq 2.0$ m, use P_r for $L = 2.0$ m.
Where P_r values are not given, the slenderness ratio exceeds 50 (maximum permitted).
- Tabulated values are valid for the following conditions:
 - standard term load (dead plus snow or occupancy loads)
 - dry service conditions
 - no fire-retardant treatment
 - $K_e = 1.0$
 - concentrically loaded
- L = unsupported length



Tension Member Selection Tables

Sawn Timber

140 mm

		Select Structural						No.1				
			T _{rN} for use with shear plates or split rings (kN)					T _{rN} for use with shear plates or split rings (kN)				
	Size (b × d)	T _r	2-5/8" SH ⌀		4" SH ⌀		T _r	2-5/8" SH ⌀		4" SH ⌀		
Species	mm	kN	1 row	2 rows	1 row	2 rows	kN	1 row	2 rows	1 row	2 rows	
D.Fir-L	140 × 140	245	196				186	148				
	140 × 191	309	264		245		234	199		185		
	140 × 241	334	295 256		279		234	207	179	195		
	140 × 292	368	332	297	318		258	233	208	223		
	140 × 343	389	357	325	344	299	272	250	228	241	209	
	140 × 394	397	369	340	357	317	278	258	238	250	222	
Hem-Fir	140 × 140	181	145				138	110				
	140 × 191	228	195		181		173	148		137		
	140 × 241	247	218	189	207		174	153	133	145		
	140 × 292	272	246	220	235		191	173	154	165		
	140 × 343	288	264	241	255	221	202	186	169	179	156	
	140 × 394	294	273	252	264	235	207	192	177	186	165	
S-P-F	140 × 140	170	136				128	103				
	140 × 191	214	182		169		162	138		128		
	140 × 241	234	207	179	195		164	145	125	137		
Northern	140 × 140	161	128				122	97.1				
	140 × 191	202	172		160		153	131		121		
	140 × 241	217	192	166	181		154	136	118	128		

Notes:

1. T_r = Factored tensile resistance based on gross area
- T_{rN} = Factored tensile resistance based on net area with one or two shear plates or split ring on each side of member at a given cross section:



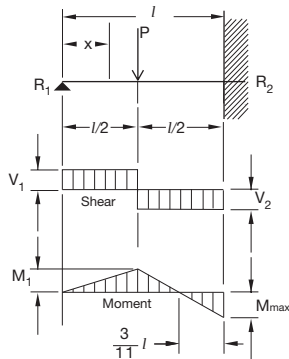
2. SH ⌀ = Shear Plate, SR = Split Ring
3. Where T_r values are not shown, area removed exceeds 25% of gross area.
4. For 4" diameter shear plates, values are based on the use of 3/4" diameter bolts.



Beam Diagrams and Formulae*

Beam Fixed at one end, Supported at Other

19.
Concentrated
load at centre



$R_1 = V_1 \dots\dots\dots = \frac{5P}{16}$

$R_2 = V_2 \text{ max.} \dots\dots\dots = \frac{11P}{16}$

$M \text{ max. (at fixed end)} \dots\dots\dots = \frac{3Pl}{16}$

$M_1 \text{ (at point of load)} \dots\dots\dots = \frac{5Pl}{32}$

$M_x \text{ (when } x < \frac{l}{2}) \dots\dots\dots = \frac{5Px}{16}$

$M_x \text{ (when } x > \frac{l}{2}) \dots\dots\dots = P \left(\frac{l}{2} - \frac{11x}{16} \right)$

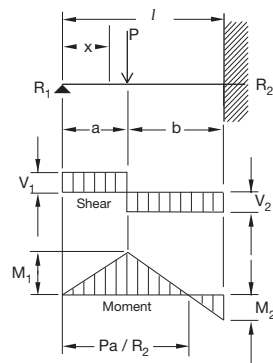
$\Delta \text{ max. (at } x = l \sqrt{\frac{1}{5}} = 0.4472l) \dots\dots\dots = \frac{Pl^3}{48EI\sqrt{5}} = 0.009317 \frac{Pl^3}{EI}$

$\Delta_x \text{ (at point of load)} \dots\dots\dots = \frac{7Pl^3}{768EI}$

$\Delta_x \text{ (when } x < \frac{l}{2}) \dots\dots\dots = \frac{Px}{96EI} (3l^2 - 5x^2)$

$\Delta_x \text{ (when } x > \frac{l}{2}) \dots\dots\dots = \frac{P}{96EI} (x-l)^2 (11x - 2l)$

20.
Concentrated
load at any point



$R_1 = V_1 \dots\dots\dots = \frac{Pb^2}{2l^3} (a + 2l)$

$R_2 = V_2 \dots\dots\dots = \frac{Pa}{2l^3} (3l^2 - a^2)$

$M_1 \text{ (at point of load)} \dots\dots\dots = R_1a$

$M_2 \text{ (at fixed end)} \dots\dots\dots = \frac{Pab}{2l^2} (a + l)$

$M_x \text{ (when } x < a) \dots\dots\dots = R_1x$

$M_x \text{ (when } x > a) \dots\dots\dots = R_1x - P(x - a)$

$\Delta \text{ max. (} a < 0.414l \text{ at } x = l \frac{l^2 + a^2}{3l^2 - a^2}) \dots\dots\dots = \frac{Pa}{3EI} \frac{(l^2 - a^2)^3}{(3l^2 - a^2)^2}$

$\Delta \text{ max. (} a > 0.414l \text{ at } x = l \sqrt{\frac{a}{2l + a}}) \dots\dots\dots = \frac{Pab^2}{6EI} \sqrt{\frac{a}{2l + a}}$

$\Delta_a \text{ (at point of load)} \dots\dots\dots = \frac{Pa^2b^3}{12EI l^3} (3l + a)$

$\Delta_x \text{ (when } x < a) \dots\dots\dots = \frac{Pb^2x}{12EI l^3} (3al^2 - 2lx^2 - ax^2)$

$\Delta_x \text{ (when } x > a) \dots\dots\dots = \frac{Pa}{12EI l^3} (l - x)^2 (3l^2x - a^2x - 2a^2l)$

Note:
* By kind permission of the American Institute of Steel Construction.

Decking Selection Tables

Select Grade

Sel

W_{FR} Maximum factored uniform load W_{FR} (kPa)*												
Span m	D.Fir-L			Hem-Fir			S-P-F			Northern		
	Thickness, mm			Thickness, mm			Thickness, mm			Thickness, mm		
	38 ¹	64	89	38 ¹	64	89	38 ¹	64	89	38 ¹	64	89
1.0	39.5			38.3			39.5			25.4		
1.2	27.4			26.6			27.4			17.6		
1.4	20.2			19.6			20.2			13.0		
1.6	15.4			15.0			15.4			9.92	31.3	
1.8	12.2			11.8			12.2	38.5		7.84	24.8	
2.0	9.88	31.2		9.58	30.3		9.88	31.2		6.35	20.1	
2.2	8.16	25.8		7.92	25.0		8.16	25.8		5.25	16.6	
2.4	6.86	21.7		6.65	21.0		6.86	21.7		4.41	13.9	28.9
2.6	5.85	18.5		5.67	17.9		5.85	18.5	38.3		11.9	24.6
2.8	5.04	15.9	33.0	4.89	15.4	32.0	5.04	15.9	33.0		10.2	21.2
3.0	4.39	13.9	28.8		13.5	27.9		13.9	28.8		8.92	18.5
3.2		12.2	25.3		11.8	24.5		12.2	25.3		7.84	16.2
3.4		10.8	22.4		10.5	21.7		10.8	22.4		6.94	14.4
3.6		9.64	20.0		9.34	19.4		9.64	20.0		6.19	12.8
3.8		8.65	17.9		8.39	17.4		8.65	17.9		5.56	11.5
4.0		7.81	16.2		7.57	15.7			16.2			10.4
4.2			14.7			14.2			14.7			9.42
4.4			13.4			13.0			13.4			8.59
4.6			12.2			11.9			12.2			7.86
4.8			11.2			10.9			11.2			7.22
5.0			10.4			10.0			10.4			6.65
5.2			9.57			9.28			9.57			6.15
5.4			8.87			8.61			8.87			5.70
5.6			8.25			8.00			8.25			5.30
5.8			7.69			7.46			7.69			4.94

W_{ΔR} Maximum specified uniform load for L/240 deflection W_{ΔR} (kPa)												
1.0	20.2			19.4			17.0			12.1		
1.2	11.7			11.2			9.81			7.01		
1.4	7.35			7.06			6.18			4.41		
1.6	4.93			4.73			4.14			2.96	16.6	
1.8	3.46			3.32			2.91	16.3		2.08	11.7	
2.0	2.52	14.2		2.42	13.6		2.12	11.9		1.51	8.50	
2.2	1.90	10.6		1.82	10.2		1.59	8.94		1.14	6.39	
2.4	1.46	8.20		1.40	7.87		1.23	6.89		0.88	4.92	13.2
2.6	1.15	6.45		1.10	6.19		0.96	5.42	14.6		3.87	10.4
2.8	0.92	5.16	13.9	0.88	4.96	13.3	0.77	4.34	11.7		3.10	8.33
3.0	0.75	4.20	11.3		4.03	10.8		3.53	9.49		2.52	6.78
3.2		3.46	9.30		3.32	8.93		2.91	7.82		2.08	5.58
3.4		2.88	7.76		2.77	7.45		2.42	6.52		1.73	4.65
3.6		2.43	6.54		2.33	6.27		2.04	5.49		1.46	3.92
3.8		2.07	5.56		1.98	5.33		1.74	4.67		1.24	3.33
4.0		1.77	4.76		1.70	4.57			4.00			2.86
4.2			4.12			3.95			3.46			2.47
4.4			3.58			3.44			3.01			2.15
4.6			3.13			3.01			2.63			1.88
4.8			2.76			2.65			2.32			1.65
5.0			2.44			2.34			2.05			1.46
5.2			2.17			2.08			1.82			1.30
5.4			1.94			1.86			1.63			1.16
5.6			1.74			1.67			1.46			1.04
5.8			1.56			1.50			1.31			0.94

¹ Thinner decking may result from remanufacturing. Loads are based on 36 mm thick decking and may be increased when the actual decking thickness is 38 mm.

* Where decking is used to support roof loads, the maximum spans for Northern Species decking may be limited by the NBCC roof point load requirements. The maximum calculated span, based on NBC roof point load requirements, for 36 mm Northern Species decking is 2.2 m. The span may be increased to 2.4 m if 38 mm thick decking is used.

2



Bending Members

Decking Selection Tables

Com**Commercial Grade****W_{FR}****Maximum factored uniform load W_{FR} (kPa)***

Span m	D.Fir-L			Hem-Fir			S-P-F			Northern		
	Thickness, mm			Thickness, mm			Thickness, mm			Thickness, mm		
	38 ¹	64	89	38 ¹	64	89	38 ¹	64	89	38 ¹	64	89
1.0	24.0			26.3			28.3			18.2		
1.2	16.6			18.3			19.6			12.6		
1.4	12.2			13.4			14.4			9.29		
1.6	9.36			10.3			11.0			7.11	22.5	
1.8	7.39			8.13			8.72	27.6		5.62	17.8	
2.0	5.99	18.9		6.59	20.8		7.07	22.3		4.55	14.4	
2.2	4.95	15.6		5.44	17.2		5.84	18.5		3.76	11.9	
2.4	4.16	13.1		4.57	14.5		4.91	15.5		3.16	9.99	20.7
2.6	3.54	11.2		3.90	12.3		4.18	13.2	27.4		8.51	17.6
2.8	3.05	9.65	20.0	3.36	10.6	22.0		11.4	23.6		7.34	15.2
3.0		8.41	17.4		9.25	19.2		9.92	20.6		6.39	13.2
3.2		7.39	15.3		8.13	16.8		8.72	18.1		5.62	11.6
3.4		6.55	13.6		7.20	14.9		7.73	16.0		4.98	10.3
3.6		5.84	12.1		6.42	13.3		6.89	14.3		4.44	9.20
3.8		5.24	10.9		5.77	11.9		6.19	12.8		3.98	8.25
4.0		4.73	9.80		5.20	10.8		5.58	11.6		3.60	7.45
4.2			8.89			9.78			10.5			6.76
4.4			8.10			8.91			9.56			6.16
4.6			7.41			8.15			8.75			5.63
4.8			6.81			7.49			8.03			5.17
5.0			6.27			6.90			7.40			4.77
5.2			5.80			6.38			6.84			4.41
5.4			5.38			5.92			6.35			4.09
5.6			5.00			5.50			5.90			3.80
5.8			4.66			5.13			5.50			3.54

W_{DR}**Maximum specified uniform load for L/240 deflection W_{DR} (kPa)**

Span m	D.Fir-L			Hem-Fir			S-P-F			Northern		
	Thickness, mm			Thickness, mm			Thickness, mm			Thickness, mm		
	38 ¹	64	89	38 ¹	64	89	38 ¹	64	89	38 ¹	64	89
1.0	17.8			17.8			15.3			11.3		
1.2	10.3			10.3			8.87			6.54		
1.4	6.47			6.47			5.59			4.12		
1.6	4.34			4.34			3.74			2.76	15.5	
1.8	3.04			3.04			2.63	14.8		1.94	10.9	
2.0	2.22	12.5		2.22	12.5		1.92	10.8		1.41	7.94	
2.2	1.67	9.37		1.67	9.37		1.44	8.09		1.06	5.96	
2.4	1.28	7.22		1.28	7.22		1.11	6.23		0.82	4.59	12.4
2.6	1.01	5.68		1.01	5.68		0.87	4.90	13.2		3.61	9.71
2.8	0.81	4.55	12.2	0.81	4.55	12.2		3.93	10.6		2.89	7.78
3.0		3.70	9.94		3.70	9.94		3.19	8.58		2.35	6.32
3.2		3.04	8.19		3.04	8.19		2.63	7.07		1.94	5.21
3.4		2.54	6.83		2.54	6.83		2.19	5.90		1.62	4.34
3.6		2.14	5.75		2.14	5.75		1.85	4.97		1.36	3.66
3.8		1.82	4.89		1.82	4.89		1.57	4.22		1.16	3.11
4.0		1.56	4.19		1.56	4.19		1.35	3.62		0.99	2.67
4.2			3.62			3.62			3.13			2.30
4.4			3.15			3.15			2.72			2.00
4.6			2.76			2.76			2.38			1.75
4.8			2.43			2.43			2.10			1.54
5.0			2.15			2.15			1.85			1.37
5.2			1.91			1.91			1.65			1.21
5.4			1.70			1.70			1.47			1.08
5.6			1.53			1.53			1.32			0.97
5.8			1.38			1.38			1.19			0.88

¹ Thinner decking may result from remanufacturing. Loads are based on 36 mm thick decking and may be increased when the actual decking thickness is 38 mm.

* Where decking is used to support roof loads, the maximum spans for decking may be limited by the NBCC roof point load requirements. Maximum calculated spans for 36 mm decking, based on NBCC roof point load requirements, are 2.0 m for D.Fir-L, 2.2 m for Hem-Fir, 2.4 m for S-P-F and 1.6 m for Northern Species. Maximum calculated spans for 38 mm thick decking are 2.2 m for D.Fir-L, 2.4 m for Hem-Fir, 2.6 m for S-P-F and 1.8 m for Northern Species.

Where the column is short, or where sheathing prevents buckling about the weak axis of the plies, P_r may be calculated as the combined factored resistance of the individual pieces taken as independent members. This will provide a larger factored resistance than calculated from the formula given above for these cases. The resistance of an individual piece may be calculated from the design formula given in Section 3.1.

Example 1: Built-up Columns

Design a built-up column for the following conditions:

- specified dead load = 1.0 kPa
- specified snow load = 2.4 kPa
- tributary area = 9 m²
- unsupported length = 3 m

- dry service conditions
- untreated
- column effectively pinned at both ends

Use Stud grade S-P-F.

Calculation

Total factored load:

$$\begin{aligned} P_f &= (1.25 \times 1.0 + 1.5 \times 2.4) \times 9 \\ &= 43.6 \text{ kN} \end{aligned}$$

From Built-up Column Selection Tables select 4-ply 38 × 140 mm:

$$P_r = 75.2 \text{ kN} > 43.6 \text{ kN} \quad \text{Acceptable}$$

Use 4-ply 38 × 140 mm Stud grade S-P-F built-up columns nailed together as shown in Figure 3.2.

where

P_f = factored axial load

e = load eccentricity

= distance between the centre of the column and the centroid of the applied load

Midway between the location where the load is applied and the column support (typically mid-height of the column) the interaction equation takes the following form when the column is designed with pinned end conditions ($K_e=1.0$).

$$\left(\frac{P_f}{P_r}\right)^2 + \frac{1}{2} \frac{P_f e}{M_r} \left[\frac{1}{1 - \frac{P_f}{P_E}} \right] \leq 1$$

Lateral Restraint

In the calculation of moment resistance for combined bending and compression, the lateral stability factor K_L may be taken as unity where lateral support is provided at points of bearing and the depth to width ratio of the member does not exceed the following values:

- 4:1 if no additional intermediate support is provided
- 5:1 if the member is held in line by purlins or tie rods
- 6.5:1 if the compressive edge is held in line by direct connection of decking or joists spaced not more than 610 mm apart
- 7.5:1 if the compressive edge is held in line by direct connection of decking or joists spaced not more than 610 mm apart and adequate bridging or blocking is installed at intervals not exceeding 8 times the depth of the member
- 9:1 if both edges are held in line

These rules apply to rectangular glulam members subjected to combined bending and compression as well as sawn lumber and timber. If the above limits are exceeded, K_L may be calculated in accordance with CSA O86 Clause 6.5.6.4.

Net Area

Members that have been drilled or bored must be designed using the net cross-sectional area. The net area A_N is calculated as follows:

$$A_N = A_G - A_R$$

where:

A_G = gross cross-sectional area

A_R = area removed due to drilling, boring, grooving or other means
 A_R must not exceed $0.25 A_G$

Only the following fasteners are considered to cause an area reduction:

- split rings
- shear plates
- bolts
- lag screws
- drift pins

The area reduction due to bolt, lag screw or drift pin holes is equal to the diameter of the hole multiplied by the thickness of the member. Table 7.2 contains area reduction information for shear plates and split rings.

Where staggered rows of fasteners are used, adjacent fasteners must be considered to occur at the same cross-sectional plane when the centre-to-centre spacing along the grain is less than the following values:

2 × fastener diameter for split rings and shear plates

8 × fastener diameter for bolts, lag screws or drift pins

Table 7.2 Area removed for shear plate and split ring joints A _R (mm ² × 10 ³)	Diameter in. Connector	Bolt	Number of faces with connector	Member thickness mm									
				38	64	80	89	130	140	175	191	215	241
Split rings													
2-1/2	1/2	1		1.11	1.48	1.71	1.84	2.43	2.57	3.07	3.30	3.65	4.02
		2		1.68	2.05	2.28	2.41	3.00	3.14	3.64	3.87	4.22	4.58
4	3/4	1		1.97	2.51	2.84	3.02	3.87	4.07	4.79	5.12	5.61	6.15
		2		3.16	3.70	4.02	4.21	5.06	5.26	5.98	6.31	6.80	7.34
Shear plates													
2-5/8	3/4	1		1.31	1.85	2.18	2.36	3.20	3.41	4.13	4.46	4.95	5.49
		2		1.84	2.37	2.70	2.89	3.73	3.94	4.66	4.99	5.48	6.02
4	3/4	1		2.12	2.65	2.98	3.17	4.01	4.22	4.94	5.27	5.76	6.30
		2		-	3.99	4.32	4.50	5.34	5.55	6.27	6.60	7.09	7.63
	7/8	1		2.19	2.80	3.18	3.40	4.38	4.61	5.45	5.83	6.40	7.02
		2		-	4.09	4.47	4.68	5.66	5.89	6.73	7.11	7.68	8.30

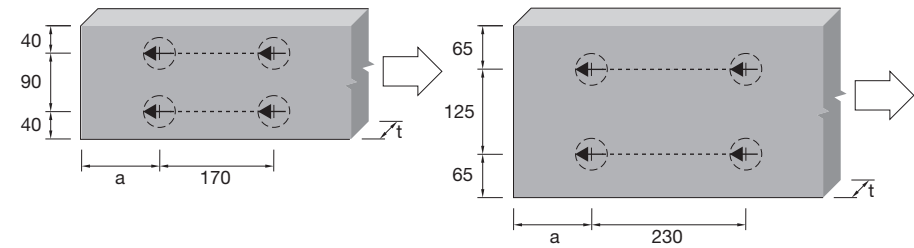
Note:
Net area for split rings and shear plates has been included in the Tension Member Selection Tables.

Figure 7.16
Minimum configuration (for $J_C = 1.0$) and minimum thickness (for $J_T = 1.0$) for split rings and shear plates

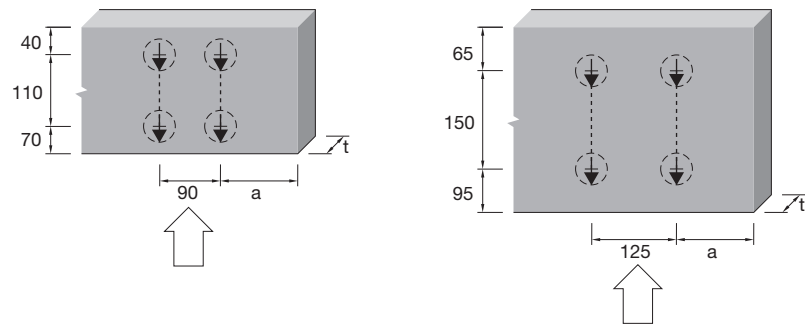
2-1/2" split rings
2-5/8" shear plates

4" split rings
4" shear plates

Load parallel to grain



Load perpendicular to grain



t = minimum thickness (mm)
a = end distance for tension members (mm)

a = 210
when t < 130

a = 270
when t < 130

a = 140
when t ≥ 130

a = 180
when t ≥ 130

t = 51 for split rings on two faces
38 for split rings on one face
64 for shear plates on one or two faces

t = 76 for split rings on two faces
38 for split rings on one face
89 for shear plates on two faces
44 for shear plates on one face

Notes:

1. All dimensions are in mm.
2. Reduced end, edge and spacing dimensions are possible; see Tables 7.22, 7.23, 7.24 and 7.25.

Sawn Timber

P_r is the lesser of:

$$P_{rd} = \phi F_c A K_{Zcd} K_{cd} \text{ or } P_{rb} = \phi F_c A K_{Zcb} K_{cb}$$

where:

ϕF_c = factored compressive resistance strength (MPa) given in Table 3.6

K_{Zc} = size factor

$$K_{Zcd} = 6.3 (dL_d)^{-0.13} \leq 1.3 \text{ for buckling in direction of } d$$

$$K_{Zcb} = 6.3 (bL_b)^{-0.13} \leq 1.3 \text{ for buckling in direction of } b$$

K_C = slenderness factor

$$K_{Cd} = \left[1.0 + \frac{F_c}{E'} K_{Zcd} C_{cd}^3 \right]^{-1} \text{ for buckling in direction of } d$$

$$K_{Cb} = \left[1.0 + \frac{F_c}{E'} K_{Zcb} C_{cb}^3 \right]^{-1} \text{ for buckling in direction of } b$$

F_c/E' = strength to stiffness ratio given in Table 3.7

$$C_{cd} = \frac{K_e L_d}{d} \quad C_{cb} = \frac{K_e L_b}{b} \quad (C_{cd} \text{ or } C_{cb} > 50 \text{ is not permitted})$$

K_e = effective length factor, given in Figure 3.1

L_b, L_d = unsupported length associated with d or b (mm)

d = depth of member (mm)

b = thickness of member (mm)

Glulam

$$P_r = \phi F_c A K_{Zcg} K_C$$

where:

ϕF_c = factored compressive resistance strength (MPa) given in Table 3.8

$$K_{Zcg} = 0.68 (Z)^{-0.13} \leq 1.0, \text{ where } Z = \text{member volume in m}^3$$

K_C = slenderness factor

$$= \left[1.0 + \frac{F_c}{E'} K_{Zcg} C_c^3 \right]^{-1}$$

F_c/E' = strength to stiffness ratio given in Table 3.9

$$C_c = \text{the greater of } \frac{K_e L_d}{d} \text{ or } \frac{K_e L_b}{b} \quad (C_c > 50 \text{ is not permitted})$$

K_e = effective length factor, given in Figure 3.1

L_b, L_d = unsupported length associated with d or b (mm)

d = depth of member (mm)

b = thickness of member (mm)

Table 3.8
Factored
compressive
strength for
glulam
 ϕF_c (MPa)

Service conditions	Dry service			Wet service		
Load duration ²	Std.	Perm.	Short term	Std.	Perm.	Short term
Compression grades						
D.Fir-L 16c-E	24.2	15.7	27.8	18.1	11.8	20.8
Spruce-Pine 12c-E	20.2	13.1	23.2	15.1	9.83	17.4

- Notes:
- For fire-retardant treated material, multiply by a treatment factor K_T . See the Commentary for further guidance.
 - Standard term loading = dead loads plus snow or occupancy loads
Permanent loading = dead loads alone
Short term loading = dead plus wind loads
 - $\phi F_c = \phi f_c K_D K_H K_{Sc} K_T$ (refer to Clause 6.5.8 of CSA O86).

Table 3.9
Modified
strength to
stiffness ratio
for glulam
 F_c / E' ($\times 10^{-6}$)

Service conditions	Dry service			Wet service		
Load duration ¹	Std.	Perm.	Short term	Std.	Perm.	Short term
Compression grades						
D.Fir-L 16c-E	80.0	52.0	92.0	66.7	43.3	76.7
Spruce-Pine 12c-E	85.3	55.5	98.1	71.1	46.2	81.8

- Notes:
- Standard term loading = dead loads plus snow or occupancy loads
Permanent loading = dead loads alone
Short term loading = dead plus wind loads
 - $F_c / E' = (f_c K_D K_H K_{Sc} K_T) / (35 E_{05} K_{SE} K_T)$ (refer to Clause 6.5.8 of CSA O86).

Modification Factors

The composite modification factors K' and J_F adjust the basic factored lateral resistance for the actual conditions of use and are calculated as follows:

$$K' = K_D K_{SF} K_T$$

$$J_F = J_E J_A J_B J_D$$

where:

K_D = duration of load factor

K_{SF} = service condition factor

K_T = fire-retardant treatment factor

J_E = factor for nailing into end grain

J_A = factor for toe nailing

J_B = factor for nail clinching

J_D = factor for diaphragm construction

In many cases K' and J_F will equal 1.0. Review the following checklist to determine if each factor is equal to 1.0. Where a factor does not equal 1.0 determine the appropriate value and calculate K' and J_F .

Nail Penetration

Minimum required penetration for single shear connections are:

- For the side member with the nail head
 - 3 nail diameters for wood members
 - 0.9mm for steel members
- 5 nail diameters for the side member with the nail point.

Minimum required nail penetration for double shear connections are

- 3 nail diameters for the member with the nail head
- 8 nail diameters for the centre member
- 5 nail diameters for the member with the point

Calculation

Try 2-1/2" common wire nails driven from alternate sides of the main member.

For double shear connections penetration into the point side member must be 5 nail diameters (15mm) or greater. The connection cannot be considered double shear.

From the Nail Selection Tables:

Minimum penetration into the main member is 16 mm and corresponding $N'_r n_s$ is 0.395 kN

Maximum penetration into the main member is 51 mm and corresponding $N'_r n_s$ is 0.544 kN

Actual penetration is 38 mm

$N'_r n_s$ based on actual penetration of 38 mm can be calculated by interpolation.

For a 38 mm penetration in the main member $N'_r n_s$ is equal to 0.489 kN.

$$N_r = N'_r n_s n_F K' J_F$$

$$N_r = 0.489 \times n_F \times 1 \times 1 = 0.489 n_F \text{ kN}$$

$$n_F \text{ required} = 8/0.489 = 16.4$$

Therefore, use seventeen 2-1/2" nails per side.

Determine minimum spacing, end distance and edge distance from Figure 7.4:

minimum spacing perpendicular to grain $c = 26 \text{ mm}$

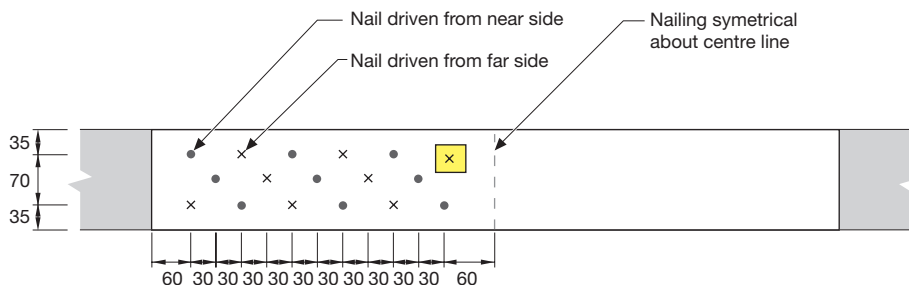
minimum edge distance $d = 13 \text{ mm}$

Therefore, use two rows of nails spaced at 70 mm, with 35 mm edge distance:

minimum spacing parallel to grain $a = 52 \text{ mm}$, use 60 mm

minimum end distance $b = 39 \text{ mm}$, use 60 mm

The final connection geometry is shown below (dimensions in mm). Note that the tensile resistance of the plywood and lumber members should also be checked.



Use seventeen 2-1/2" common nails.

Modification Factors

The composite modification factors K' and J_F adjust the basic factored lateral resistance for the actual condition of use and are calculated as follows:

$$K' = K_D K_{SF} K_T$$

$$J_F = J_E J_A$$

where:

K_D = duration of load factor

K_{SF} = service condition factor

K_T = fire-retardant treatment factor

J_E = factor for fastening into end grain

J_A = factor for toe-screwing

In many cases K' and J_F will equal 1.0. Review the following checklist to determine if each factor is equal to 1.0. Where a factor does not equal 1.0 determine the appropriate value and calculate K' and J_F .

Screws may be designed for withdrawal under wind or earthquake loads only. Design requirements for withdrawal are given in CSA O86 Clause 10.11.5. The factored withdrawal resistance is the lesser of the factored withdrawal resistance of the main member, $P_{rw'}$ or the head pull-through resistance of the side member, P_{pt} . Withdrawal resistance of the main member is given in Table 7.4 and head pull-through resistance of the side member is given in Table 7.5.

Minimum required penetration for single shear connections are:

- **The side member with the screw head:**
 - **3 screw diameters for wood members**
 - **0.9mm for steel members**

Minimum required penetration for double shear connections are:

- **3 screw diameters for the side members with the screw head**
- **8 screw diameters for the centre member**
- **5 screw diameters for the side member with the screw point.**

Calculation

Try 6 gauge 2" screws driven from alternate sides of the main member.

For double shear connections, penetration into the point side member must be 5 screw diameters (17.5mm) or greater. The connection cannot be considered double shear.

From the Screw Selection Tables:

Minimum penetration into the main member is 18 mm and corresponding $N'_r n_s$ is 0.373 kN

Maximum penetration into the main member is 40 mm and corresponding $N'_r n_s$ is 0.546 kN

Actual penetration is 38 mm.

$N'_r n_s$ based on an actual penetration of 38 mm can be calculated by interpolation.

For a 38 mm penetration in the main member $N'_r n_s$ is equal to 0.530 kN.

$$N_r = N'_r n_s n_F K' J_F$$

$$N_r = 0.530 \times n_F \times 1 \times 1 = 0.530 n_F \text{ kN}$$

$$n_F \text{ required} = 8/0.530 = 14.1$$

Therefore use sixteen 2" screws per side

Determine minimum spacing, end distance and edge distance from Figure 7.5:

Minimum spacing perpendicular to grain $c = 28 \text{ mm}$

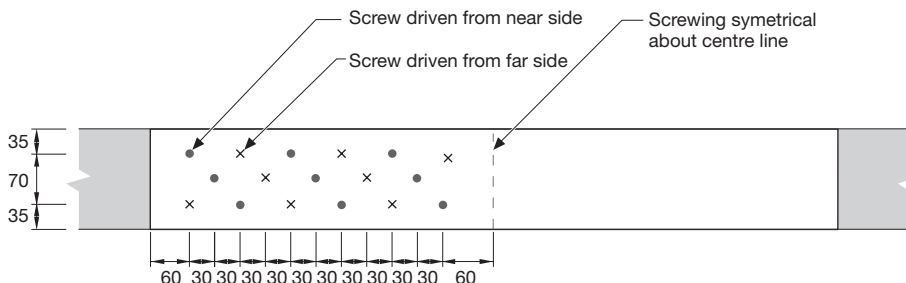
Minimum edge distance $d = 14 \text{ mm}$

Therefore, use two rows of screws spaced at 70 mm, with 35 mm edge distance:

Minimum spacing parallel to grain $a = 56 \text{ mm}$, use 60 mm

Minimum end distance is 42 mm, use 60 mm

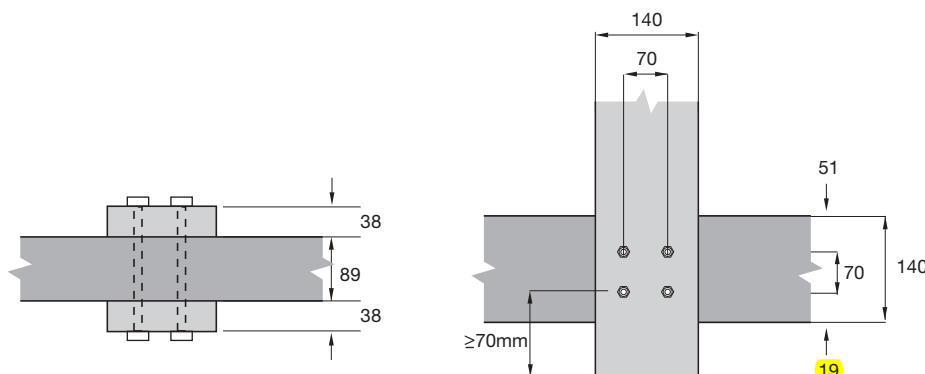
The final connection geometry is shown below (dimensions in mm). Note that the tensile resistance of the OSB and lumber members should also be checked.



Use sixteen 6 gauge 2" screws.

Example 2: Bolts

Determine if two rows of 1/2" bolts are adequate for the attachment of the beam to the wooden tension member. The wood tension member consists of two 38 x 140 mm D.Fir-L No. 2 grade sawn lumber members. The beam is 89 x 140 mm D.Fir-L No. 2 grade sawn lumber. The total factored tension force is 20 kN.



Modification Factors

$K_D = 1.0$ (loading is standard term)

$K_{SF} = 1.0$ (service conditions are dry, material is seasoned)

$K_T = 1.0$ (wood members are not treated)

Therefore:

$$K' = 1.0$$

Calculation

The configuration is Type 5 – double shear with wood side plates loaded parallel to the grain and the main member loaded perpendicular to grain.

Try two rows of two 1/2" diameter bolts:

P_r is equal to the lesser of row shear resistance, PR_{rT} , group tear-out resistance PG_{rT} , and tension resistance parallel to grain.

Q_r is equal to perpendicular to grain splitting resistance QS_{rT} .

The maximum bolt spacing parallel to grain is $140 - 19 - 51 = 70$ mm.

For an efficient connection, the loaded end distance should be the same as the bolt spacing parallel to grain. The spacing between rows of bolts is 70 mm.



The factored shear resistance of panels on both sides of the same shearwall may be added together. Where wood structural panel are applied over 12.7 mm or 15.9 mm thick gypsum wallboard, the shear resistance of the wood-based panel may be considered in the shearwall design, provided minimum nail penetration requirements are met. In all other cases with multiple layers of panels on the same side of the shearwall, only the shear resistance of the panel closest to the studs is considered in design.

Shearwalls With Segments

Where shearwalls have openings for windows or doors, only the full height shearwall segments between the openings and at the ends of the shearwalls are considered in the shearwall design. **In the case of blocked shearwalls** where the height of the shearwall segment, H_s , measured from the bottom of the bottom plate to the top of the top plate, is greater than 3.5 times the length of the shearwall segment, L_s , the segment is not included in the resistance calculation. **For unblocked shearwalls, where H_s is greater than $2L_s$, the segment is not included in the resistance calculation.**

A shearwall is designed to resist the sum of factored shear forces from upper storey shearwalls and diaphragms. Where materials or construction details vary between shearwall segments, the capacity of the shearwall may either be conservatively estimated based on the minimum segment capacity. Alternatively the total factored shear force on the shearwall, V_{fs} , may be distributed to each of the segments. Different methods are used to distribute the shear force on a shearline to each of the shearwall segments. The distribution of lateral forces to the shearwall segments may be based on the relative strength or relative stiffness of the segments. See the information on Lateral Force Distribution to Shearwall Segments later in this section.

The shearwall sheathing and the connection of the sheathing to the framing members must be designed so that the factored shear resistance of the shearwall segment per unit length, v_r , is equal to or greater than the maximum shear force in the shearwall segment per unit length, v_{fsi} . The maximum shear force is assumed to be uniformly distributed the full length of the shearwall

segment parallel to the applied load, L_s , and $v_{fsi} = \frac{V_{fsi}}{L_s}$.

Capacity of shearwalls may vary with load direction and shearwalls must be designed for lateral loads acting in opposite directions. The resistance on the shearwall in each direction must be greater than the corresponding lateral load.

Shearwall Segments Without Hold-downs

Traditionally, shearwalls have been designed using chords and hold-down connections at the ends of all shearwall segments. Hold-downs are designed to transfer the chord segment overturning force, T_p , to the shearwall or foundation below. CSA O86 includes provisions for design of shearwall segments without hold-down connections.

Without hold-downs, the overturning tension force is transferred from the top wall plate to the bottom wall plate through the shearwall sheathing. Since a portion of the shearwall sheathing is used to resist the overturning force, the shear capacity of the sheathing is reduced. Even though hold-down anchors are not used, anchorage is still required to transfer the uplift force from the wall plate to the foundation or shearwall below (see Commentary).



2. Adequate shear resistance must be provided

a) For sawn timber and SCL:

Factored shear resistance $V_r \geq$ maximum factored shear force V_f

In the calculation of V_f , loads within a distance from the support equal to the depth of the member may be neglected.

For sawn timber only, factored notch shear force resistance $F_r \geq$ maximum reaction force Q_f when a member has a notch on the tension side at a support.

b) For glulam only:

i) Beams with a volume less than 2.0 m^3

If the beam volume is less than 2.0 m^3 , shear resistance may be checked by the procedure described in ii) or the tabulated shear resistance V_r may simply be compared to the maximum factored shear force V_f . In the calculation of V_f , loads within a distance from the support equal to the depth of the member may be neglected.

ii) Beams of any volume

Shear resistance $W_r \geq$ total of all factored loads acting on beam W_f

where:

$$W_r = (W_r L^{0.18}) L_o^{-0.18}$$

$(W_r L^{0.18})$ = unit factored shear resistance from Beam Selection Tables

L_o = beam length in m

3. Factored bearing resistance $Q_r \geq$ maximum factored reaction Q_f (refer to Chapter 6)

4. Maximum deflection under specified loads < deflection criteria (actual $E_S I >$ required $E_S I$)

Examples:

For L/180 deflection limit based on total load:

$$E_S I_{REQ'D} = 180 \left[\frac{5wL^3}{384} \right]$$

For L/360 deflection limit based on live load:

$$E_S I_{REQ'D} = 360 \left[\frac{5w_L L^3}{384} \right]$$

where:

w = total specified load

w_L = specified live load

The Beam Selection Tables for sawn timbers and SCL provide M_r , V_r and $E_S I$ values.

The Beam Selection Tables for glulam provide M'_r , V_r and $E_S I$ values. To obtain M_r for glulam, multiply M'_r (from the Glulam Beam Selection Tables) by the lesser of K_L (from Table 2.9) or K_{Zbg} (from Table 2.10).

Note that in certain cases the *National Building Code of Canada* permits a reduction in the loads due to use and occupancy depending upon the size of the tributary area (refer to Article 4.1.6.9 of the *NBCC*).

Modification Factors

The tabulated resistances for sawn timber and glulam are based upon the following formulae and modification factors. When using the tables, be certain that the member conforms exactly to the modification factors used in the tables; if not, use the factors below and make the necessary adjustments to the tabulated values.

For sawn timbers:

$$M_r = \phi F_b S K_{zb} K_L \text{ (N}\cdot\text{mm)}$$

$$V_r = \phi F_v \frac{2A_n}{3} K_{zv} \text{ (N)}$$

$$F_r = \phi F_f A K_N \text{ (N) for beams with notches on the tension side at supports}$$

For straight glulam:

$$M_r = \text{lesser of } M'_r K_L \text{ or } M'_r K_{Zbg} \text{ (N}\cdot\text{mm)}$$

$$M'_r = \phi F_b S \text{ (N}\cdot\text{mm)}$$

$$V_r = \phi F_v \frac{2A}{3} K_N \text{ (N)}$$

$$W_r = \phi F_v 0.48 A K_N C_v Z^{-0.18} \text{ (N)}$$

which may be expressed as:

$$W_r L^{0.18} = \phi F_v 0.48 A K_N C_v (b d)^{-0.18} \text{ (N}\cdot\text{m}^{0.18})$$

(as shown in the Beam Selection Tables)

For sawn timber and glulam:

$$E_S I = E (K_{SE} K_T) I \text{ (N}\cdot\text{mm}^2)$$

Table 2.10
Values of K_{zbg}
for glulam
beams

L m	B (mm)						
	80	130	175	215	265	315	365
3	1	1	1	1	1	1	1
3.5	1	1	1	1	1	1	0.986
4	1	1	1	1	1	0.988	0.962
4.5	1	1	1	1	0.998	0.967	0.942
5	1	1	1	1	0.979	0.949	0.924
5.5	1	1	1	1	0.962	0.933	0.909
6	1	1	1	0.984	0.948	0.918	0.894
6.5	1	1	1	0.970	0.934	0.905	0.882
7	1	1	0.993	0.957	0.922	0.893	0.870
7.5	1	1	0.981	0.945	0.910	0.882	0.859
8	1	1	0.969	0.934	0.900	0.872	0.849
8.5	1	1	0.959	0.924	0.890	0.863	0.840
9	1	1	0.949	0.915	0.881	0.854	0.831
9.5	1	0.992	0.940	0.906	0.872	0.846	0.823
10	1	0.982	0.931	0.897	0.864	0.838	0.816
10.5	1	0.974	0.923	0.890	0.857	0.830	0.809
11	1	0.966	0.915	0.882	0.850	0.824	0.802
11.5	1	0.958	0.908	0.875	0.843	0.817	0.796
12	1	0.951	0.901	0.868	0.836	0.811	0.790
12.5	1	0.944	0.895	0.862	0.830	0.805	0.784
13	1	0.937	0.888	0.856	0.824	0.799	0.778
13.5	1	0.931	0.882	0.850	0.819	0.794	0.773
14	1	0.925	0.877	0.845	0.813	0.789	0.768
14.5	1	0.919	0.871	0.839	0.808	0.784	0.763
15	0.997	0.913	0.866	0.834	0.803	0.779	0.758

Notes:

1. B is the member width for single piece laminations, mm. For laminations consisting of multiple pieces, B is the width of the widest piece. Glulam laminations wider than 175 mm are typically constructed with multiple pieces. Check with glulam supplier.
2. L is the length of the glulam from point of zero moment to zero moment, m. For simple span beams, L is the span of the beam.
3. $K_{zbg} = 1.03(B/1000 \times L)^{-0.18}$ but not greater than 1.0.
4. Use the lesser of K_{zbg} and K_L to determine M_r .



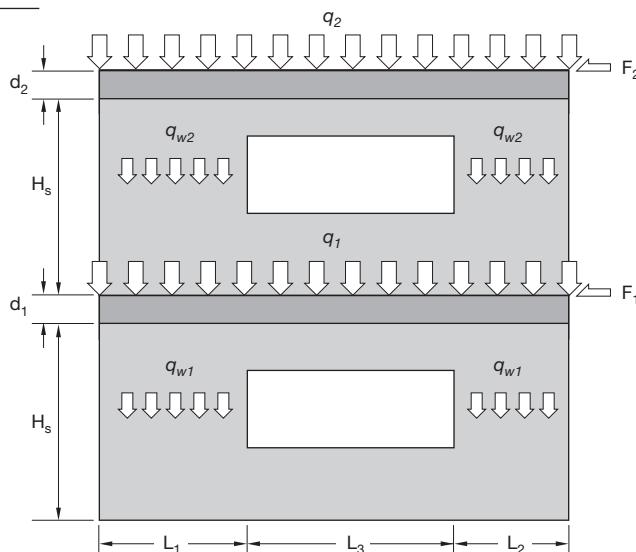
In the lower storeys of a structure:

P_{tj} = the factored floor dead load acting on the top of the end stud in the shearwall segment minus R_j from the storey above (kN)

P_j = P_{tj} + the factored wall dead load acting at the bottom of the end stud in the shearwall segment (kN)

$$R_j = \frac{V_{fsi}(H_s + d)}{L_s} - P_j \text{ (kN)}$$

Figure 8.5
Steps in
Calculation
of J_{hd}



Steps:

Calculate J_{hd} for all segments of the upper storey shearwall before proceeding to the next lower storey.

1. Divide the shearwall into segments (L_1 , L_2)
2. Calculate the dead load to resist overturning at the top of the segments (P_{tj}), and the bottom of the segments (P_j).
3. Calculate J_{hd} for each of the segments.
4. Calculate the shear resistance of each segment (V_{rs}).
5. Distribute the storey shear load (V_{fs}) to the segments based on their relative resistance.
6. Calculate the resultant overturning force at the end of each segment (R_j).
7. Repeat steps 2 to 6 for lateral loads acting in the opposite direction.
8. Repeat steps 1 to 7 for each lower storey shearwall.

Hold-down connections are required at the ends of each wall segment to resist the R_1 uplift forces. If the hold-down connections are installed at the ends of each of the shearwall segments, they may be designed to resist the R_1 uplift forces shown above. In general, if the hold-down connections are offset from the ends of the shearwall segments, the hold-down forces are calculated as:

$$T_f = \frac{V_{fs1}(H_s + d)}{h} - P_i$$

where:

h = centre-to-centre spacing between stud chords

Lateral Force Distribution to Shearwall Segments

Different methods are used to distribute the shear force on a shearline to each of the shearwall segments. The distribution of lateral forces to the shearwall segments may be based on the relative strength of the segments. This approach is less accurate than distributing forces based on the relative stiffness of the segments. Distributing forces by the relative strength of the segments is improved when the segments in the shearwall have similar configurations and ductility.

The most rigorous approach is to distribute the forces based on the relative stiffness of each segment using the shearwall deflection equations to determine the stiffness of each segment. This approach typically requires an iterative process to arrive at a solution where all of the segments in the shearwall have the same displacement at the load level being considered.

Example 2: Methods of lateral force distribution to a line of shearwall segments.

Determine the forces in the one storey office building shearwall shown below for the following conditions:

Design information:

- dry service conditions ($K_{SF} = 1$)
- factored roof diaphragm wind load reaction (F) = 42 kN
- specified roof diaphragm wind load reaction = 30 kN
- specified shearwall force, $V_{fs} = 30$ kN
- walls are 3 m high
- depth of the roof framing is 0.3 m

